### PLANETARY PRECESSIONAL TRANSMISSIONS: GENERATION TECHNOLOGIES

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#### 1. INTRODUCTION

A problem for engineering companies (especially the metalworking industry, in automotive, chemical and metallurgical industries) is to satisfy the ever-increasing requirements to the transmissions used in majority of industrial machinery and technological equipment related to compactness, bearing capacity, mass dimensions, low cost of production, etc., and, in particular, to kinematical characteristics, structural compatibility with other aggregates of the equipment, etc. Gearings are considered the most sophisticated components of machines. Machine reliability depends very much on the gearing mechanical transmission operation, in general. The quality indices of traditional gears were increased largely by changing involute gearings, and by creating new gearings, such as Novikov-Hlebanija Symark, etc.

In the field of planetary transmission it was considered properly to follow the way of developing new types with increased performances. Scientific analysts consider that in the field of technical sciences worldwide an essentially new type of mechanical transmission is being invented every 20-25 years. Thus, the German engineer L. Braren developed the cvcloid planetary transmission "CYCLO" in 1923. The Russian engineer A. Moskvitin invented the harmonic friction transmission in 1944 and in 1959 the American engineer C.W. Musser developed the harmonic gear transmission.

In the late 70ies a new type of mechanical transmission has been developed at the Polytechnic Institute of Chisinau (now the Technical University of Moldova). The new type of mechanical transmission entered into international terminology circuit as planetary precessional transmission (PPT). The first patent was issued under this name in 1983 [1,2,3,4]. Planetary precessional transmission differs from the classical one by the new principle of motion and load transformation and transmission, i.e. by using sphere-spatial motion of the satellite and variable convex – concave profile. Due to these innovative features gearing multiplicity in planetary precessional transmission reaches 100% (in

classical transmissions - 3-7%) which provides increased bearing capacity, reduced dimensions and weight, extended kinematical range  $\pm$  10 ...  $\pm$  3599 (in harmonic transmissions 79 ... 300), high kinematical accuracy, etc. The research team involved in research on precessional planetary transmissions published over 800 scientific articles, obtained about 170 patents, implemented about 20 practical achievements in the field of fine mechanics and specialized technological equipment, in robotic complexes for the exploration of ferro-manganese concretions from the World Ocean bottom (USSR concept), in spaceflight technique, etc.

<u>Know-how</u> in the elaboration of multicouple precessional gear, manufacturing technology and control methods, and a range of precessional transmission diagrams belong to the research team from the Technical University of Moldova.

- The specific character of sphere-spatial (precessional motions of the precessional transmissions pinion make impossible the utilisation of classical involute teeth profiles. This fact requires the elaboration of new profiles adequate to the sphere-spatial motion of pinion, which would ensure high performances to the precessional transmission. Carrying out on the principle of the transfer function continuity and gear [1,2] based on the principles of the transfer function continuity and gear multiplicity which aims to:
- the elaboration of the gear mathematics model with account of the peculiarities;
- the analytical description of teeth profiles by a system of parametric equations on spherical surface and normal teeth section for inner and plane gear;
- CAD determination of geometrical and cinematic parameters influence of the gear upon the teeth profiles shape and the justification of their rational limits of variation;
- the elaboration of the theoretical basis evaluation of teeth gear multiplicity in precessional transmissions:
- area definition of gear multiplicity existence by 100% teeth couples.
- the production of non-standard teeth profiles requires a new manufacturing technology. In the

complexity of problem "gear-synthesis-profile study- manufacturing" the elaboration of efficient methods of teeth manufacturing which ensures a maximum productivity and reduced cost while satisfying the requirements related to the gear with precessional motion plays an important role. To solve this problem the following has been done:

- we elaborated the mathematical model of teeth generation which shows the interaction of teeth in precessional gear;
- we investigated the kinematics of the mechanism of method realisation for teeth generation;
- we determined the tool path of motion and the family envelope of the generating surface by using the computer;
- we elaborated and manufactured from metal milling and tooth grinding tools, inclusively their longitudinal modification.

#### 2. GENERATION TECHNOLOGIES

#### 2.1. General remarks

Development of mechanical transmission with gear, different from the classical one, requires complex research in various fields. This finding refers to planetary precessional transmission with multicouple gear, which is characterized by essential constructive-kinematical features. In solving complex problems related to "gear synthesis - profile research – fabrication" an important role belongs to developing efficient methods of teeth manufacturing, which would ensure maximum productivity, reduced cost and quality.

Manufacture of precessional gear wheels with convex-concave and variable tooth profile cannot be achieved by existing generation technologies, but through fundamentally new technology. Generation technology of precessional wheel teeth must ensure continuity of motion transformation function with the following conditions: non-standard and variable tooth profile, and satellite carrying out spherespatial motion with a fixed point. To achieve the above, a new procedure for teeth processing is proposed by self-generating method with precessional tool against rotating blank [4].

To develop the theoretical basis for generating tooth profile by running the precessional tool it is necessary to determine the character of continuous contact of the tool cutting edge and profile of the processed wheel tooth for a complete "tool-blank" precessional cycle. In this connection a mathematical model of tooth self-generating

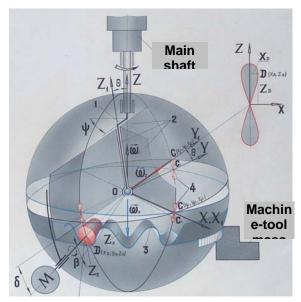
method by running the precessional tool was elaborated, which fully reflects the actual interaction of teeth in precessional transmission. For this purpose the following was described:

- kinematical connection of the precessional tool with the blank that ensures continuity of motion transformation function in the linkage "tool-blank";
- path of motion of the tool centre in the fixed system of coordinates;
- path of motion of the tool centre in the movable system of coordinates, connected with the rotating blank;
- the generating contour of the tool in the movable system of coordinate and the system envelope of generating surfaces of the tool for a cycle of precession;
- projection of tool contour envelope in the plane system of coordinates.

# 2.2. Technological system for teeth generation by sphere-spatial motion of tool as truncated cone

#### 2.2.1. Kinematics of gear generation system

To achieve teeth generation method a tool carrier device was developed, which diagram is shown in Fig. 1. In the designed device the node, which involves the tool in sphere-spatial motion, is stopped from rotating around the common axis of the main shaft-blank - a kinematic joint. Rotation of blank 3 and main shaft 1 is coordinated by the



**Figure 1.** Principled spatial diagram of teeth processing method by precessional tool running

division kinematic chain of machine tool. Kinematic joint of tool with the body must be built so as to ensure continuity of the transmission function of rotation motion, i.e.  $\omega_1/\omega_3 = const$ . Continuity of transmission function of rotation motion is determined by path of motion of point C, belonging to the movable system of coordinates. To research the kinematics of the device that involves the tool in precessional motion: Imaginary satellite gear (profile generating tool) 2 with an imaginary number of teeth  $Z_2$  (determined by the machine-tool kinematics) gears with the blank 3, fixed on machine-tool table, with the number of teeth  $Z_2=Z_2\pm I$ . At a turning of the main shaft 1 the blank rotates at angle  $\psi_3$ , that corresponds to the angle between the difference of the wheel teeth:

$$\psi_3 = \frac{2\pi}{Z_3} (Z_2 - Z_3). \tag{1}$$

To define the position function of the given device  $\psi_3 = f(\psi)$  it is necessary to determine beforehand the equations of the tool motion in the fixed OXYZ and movable  $OX_IY_IZ_I$  systems of coordinates. The link between the mentioned systems of coordinates is determined by the Euler angles. Sphere-spatial motion of tool (imaginary wheel) at uniform rotation of the main shaft 1  $\omega_I$  is described by the system of equations

$$\psi = \omega_1 t, \quad \theta = const., \quad \varphi = \varphi(t),$$
 (2)

Design of the working device for teeth generating technology should provide limitation of tool rotation around the main shaft of the tool-machine by a certain technical solution, for example by kinematical coupling "bolt-gutter".

In this case the coordinates of the bolt contact point C (fig.2) with the groove in the movable system of coordinates OX1Y1Z1 will be:

$$X_{1C} = 0,$$
  $Y_{1C} = R_c,$   $Z_{1C} = 0,$  (3)

where  $R_c$  is the radius of point C location.

At sphere-spatial motion of tool 2, the motion of point C located in plane OZX is limited by the groove walls, i.e. the condition is realised for each value of  $\psi$ :

$$X_C = 0. (4)$$

Using the transition matrix of the movable system of coordinates  $OX_1Y_1Z_1$  connected with the tool and the bolt limiting its rotation around the shaft Z in the fixed system of coordinates, condition  $X_c = 0$  o can be written in the form:

$$X_{c} = \begin{vmatrix} X_{tc} \\ Y_{tc} \\ Z_{c} \end{vmatrix} = 0.$$
 (5)

Or in extended form>

$$X_c = a_{11}X_{1c} + a_{12}Y_{1c} + a_{13}Z_{1c} = 0$$

By replacing  $a_{11}$ ,  $a_{12}$  and  $a_{13}$  in (4) we obtain:

$$X_{c} = X_{lc} (\cos \psi \sin \varphi - \sin \psi \sin \varphi \cos \theta) -$$

$$-Y_{lc} (\cos \psi \sin \varphi + \sin \psi \cos \varphi \cos \theta) + Z_{lc} \sin \psi \sin \theta = 0$$
(6)

For the contact point of the bolt with the groove coordinates (5) we have:

$$X_c = -R_c (\cos \psi \sin \varphi + \sin \psi \cos \varphi \cos \theta) = 0.$$
 (7)

Thus, 
$$(\cos\psi\sin\phi + \sin\psi\cos\phi\cos\theta) = 0$$
. (8)

By solving equation (8) we determine the linkage equation between the angle of tool self-rotation 2 and the angle of rotation of the main shaft:

$$\varphi = -arctg(\cos\theta tg\psi). \tag{9}$$

In such case the equations of tool 2 precessional motion take the form:

$$\psi = \omega_t t$$
,  $\theta = const.$   $\varphi = -arctg(cos \theta \cdot tg\psi)$ . (10)

To establish the dependence of the angle of rotation of blank  $\psi_3$  on the angle of rotation of the main shaft  $\psi$  we describe the blank motion composed of the involved rotational motion with the crank of the main shaft  $\psi_{3e}$  and the relative motion of rotation with regard to the crank of the main shaft  $\psi_{3r}$ .

In the compound motion of blank  $\psi_{3e} = \psi$ , and  $\psi_{3r}$  represents a certain function  $f(\varphi)$  of the angle of rotation of tool  $\varphi$ , that is:

$$\psi_3 = \psi + f(\phi). \tag{11}$$

For ideal precession of the drive mechanism of machine/tool function  $f(\varphi)$  will take the form:

$$\psi_3 = \psi + \frac{Z_2}{Z_1} \varphi \,. \tag{12}$$

By considering equation (9) we obtain the position function of the kinematical linkage mechanism of the device:

$$\psi_3 = \psi - \frac{Z_2}{Z_1} \arctan(\cos\theta t g \psi). \tag{13}$$

Momentary gear ratio of the kinematical linkage mechanism of the device is obtained deriving (13) after  $\psi$ :

$$i_{31} = \frac{d\psi_3}{d\psi} = \frac{\omega_3}{\omega_1} = 1 - \frac{Z_2}{Z_3} \cdot \frac{\cos\theta}{\cos^2\psi + \cos^2\theta\sin^2\psi}.$$
 (14)

Average gear ratio for a rotation of the main shaft will be

$$i_{31}^{med} = \frac{1}{2\pi} \int_{0}^{2\pi} i\psi d\psi =$$

$$= \frac{1}{2\pi} \left[ \psi - \frac{z_{2}}{z_{3}} \arcsin(\cos\theta t g\psi) \right] \Big|_{0}^{2\pi} = -\frac{Z_{2} - Z_{3}}{Z_{3}}.$$
(15)

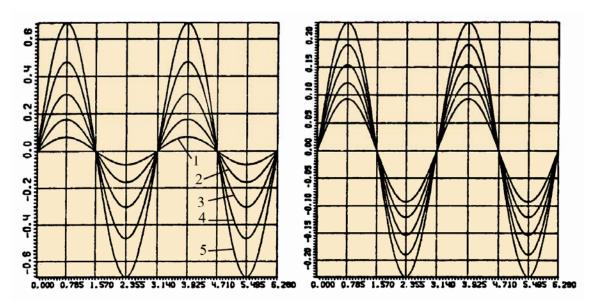
Analysis of dependence (15) demonstrates that for the ratio of teeth  $z_2 < z_3$  the direction of main shaft rotation of gear cutting machine and blank (imaginary wheel) coincides, and for the ratio of teeth  $z_2 > z_3$  is different. Division kinematical chain of machine tool must provide the following kinematical link: at full rotation of the main shaft the blank (imaginary wheel) should rotate under angle  $\psi_3 = 2\pi (Z_2 - Z_3)/Z_3$ . This kinematical link defines the average gear ratio of the manufactured gear. Given the fact that the kinematical link "tool – blank" is done by the machine - tool dividing chain under condition  $\omega_1/\omega_2 = const.$ , the angular velocity variation caused by the kinematic link mechanism of the tool with the frame will transpose on the

tooth profile, therefore, it will introduce a diagram error  $\Delta \psi_3$  in the tooth profile. The diagram error  $\Delta \psi_3$  can be identified by angular positioning error of the blank  $\psi_3$  relative to position  $\psi_3^{med}$  of the same blank, which conditionally would rotate uniformly with the gear ratio  $i_{31}^{med} = -(Z_2 - Z_3)/Z_3$ . in this case the diagram error will be:

$$\Delta \psi_3 = \psi_3 - i_{31}^{med} = \frac{Z_2}{Z_3} \left[ \psi - arctg(\cos\theta tg\psi) \right]. \tag{16}$$

So, the kinematical link of the tool with the frame introduces some diagram error in the tooth profile.

Fig. 2 shows the graph of diagram error of tool position error  $\psi_3$  at one rotation of the main shaft and motion of point D in OZY plan. If point C makes a motion in OZY plane the error is transmitted intact to the tool, and the last generates the tooth profile with the same error. To ensure continuity to motion processing function it is necessary to modify the tooth profile by diagram error value  $\Delta \psi_3$  by communicating additional motion to the tool.



**Figure 2.** Dependence of tool position error on the angle of rotation  $\psi$  of the main shaft for various angles of

Correctness of additional motion of the tool was established using a computer calculation program. It was found that generation precision of the manufactured wheel teeth 3 depends on the continuity of its angular speed  $\dot{\varphi}$  of the tool 2. Function analysis (12) shows that for  $\varphi = -\psi$  the instantaneous transmission ratio  $i_{31} = const$ . For condition  $\varphi = -\psi$  from equation (12) we have:

$$\psi_3 = \psi - \frac{Z_2}{Z_3} \varphi = \frac{Z_2 - Z_3}{Z_3} \psi = \frac{Z_2 - Z_3}{Z_3} \omega_l t.$$

From this analysis we find that any technical solution to eliminate the influence of diagram error of tooth profile precision generation with precessional tool would be 3D profiling of the contact surfaces of the groove of kinematical link mechanism, which supports the bolt (delimiter of rotation). The bolt contact with the shaped surfaces

of groove transmits also the reaction torque from the node, on which the tool is installed to the frame. To achieve the proposed technical solution to exclude the error of 3D profiling of supporting surface of the link channel with the bolt it is necessary to describe the profile of contact surfaces with parametric equations. In this case we take an arbitrary point C on the tool axis with coordinates  $X_{Ic}$ ,  $Y_{Ic}$ ,  $Z_{Ic}$  (Fig. 1), and identify the path of motion in the fixed system of coordinates OXYZ to satisfy the condition  $i_{3I}$ =const. Using the matrix form for the transition from the coordinate system  $OX_IY_IZ_I$  to the fixed system OXYZ we get:

or by components:

$$X_{c} = a_{11}X_{1c} + a_{12}Y_{1c} + a_{13}Z_{1c};$$

$$Y_{c} = a_{21}X_{1c} + a_{22}Y_{1c} + a_{23}Z_{1c}; \dots (18)$$

$$X_{c} = a_{31}X_{1c} + a_{32}Y_{1c} + a_{33}Z_{1c}.$$

where  $a_{i,j}$ , i,j = 1...3 are cosines of angles between the axes of coordinates.

Considering that instantaneous gear ratio  $i_{3l}$ =const. when  $\varphi = -\psi$  then equations (18) are transcribed as:

$$\begin{split} &X_{C} = X_{IC}(\cos^{2}\psi + \cos\theta\sin^{2}\psi) + Y_{IC}(1 - \cos\theta)\cos\psi\sin\psi + Z_{IC}\sin\theta\sin\psi, \\ &Y_{C} = Y_{IC}(1 - \cos\theta)\cos\psi\sin\psi + Y_{IC}(\sin^{2}\psi + \cos\theta\cos^{2}\psi) - Z_{IC}\sin\theta\cos\psi, \\ &Z_{IC} = Z_{IC}\sin\theta\sin\psi + Y_{IC}\sin\theta\cos\psi + Z_{IC}\cos\theta. \end{split}$$

For the case when point "C" is placed on axis  $OY_I$  its position is defined by coordinates  $X_{1C} = 0$ ,  $Y_{1C} = R_c$ ,  $Z_{1C} = 0$ , and equations (19) take the form:

$$X_{C} = R_{C}(1 - \cos\theta)\cos\psi\sin\psi;$$

$$Y_{C} = R_{C}(\sin^{2}\psi + \cos\theta\cos^{2}\psi);$$

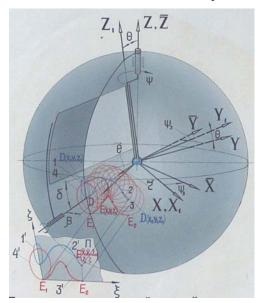
$$Z_{C} = R_{C}\sin\theta\sin\psi.$$
(20)

Equations (20) represent parametrical equations of groove lateral surfaces, by which the limiting bolt of tool rotational motion around the fixed axis OZ, form a kinematical coupling, and provides the condition  $i_{31}$ =const. Thus, the shape of groove lateral surfaces by which the bolt forms the kinematical coupling of tool with the casing, described by parametrical equations (20), excludes the influence of diagram errors on tooth profile generated with precessional tool.

### 2.2.2. Analytical description of the precessional tool path of motion

According to the principle of teeth generation

by proposed method the tool should copy with certain accuracy the shape and path of motion of the pin tooth in the real gearing (involving the central wheel with teeth – satellite gear with pin teeth). In this connection it was necessary to research the tool path of motion with the angle of position to the blank  $\delta \ge 0$ . For this purpose, a point D was identified on the tool axis (fig. 3) with coordinates  $X_{ID}$ ,  $Y_{ID}$ ,  $Z_{ID}$  in the movable system of coordinates  $OX_1Y_1Z_1$  and parametrical



**Figure 3.** Determination of the tool surface family envelope.

equations of its motion in the movable system of coordinates were described. For  $i_{3l}$ -const. after a number of transformations we obtain:

$$X_{D} = \alpha_{11}X_{1D} + \alpha_{12}Y_{1D} + \alpha_{13}Z_{1D};$$

$$Z_{D} = \alpha_{21}X_{1D} + \alpha_{22}Y_{1D} + \alpha_{23}Z_{1D};$$

$$Z_{D} = \alpha_{31}X_{1D} + \alpha_{23}Y_{1D} + \alpha_{33}Z_{1D}.$$
(21)

With condition  $\varphi = -\psi$  and constant instantaneous gear ratio  $i_{3l}$ -const we have:

$$\begin{split} X_{D} &= X_{ID}(\cos^{2}\varphi + \cos\Theta\sin^{2}\varphi) + Y_{ID}(1 - \cos\Theta)\cos\varphi\sin\varphi + Z_{ID}\sin\Theta\sin\varphi; \\ Y_{D} &= X_{ID}(1 - \cos\Theta)\sin\varphi\cos\varphi + Y_{ID}(\sin^{2}\varphi + \cos\Theta\cos^{2}\varphi) - Z_{ID}\cos\varphi\sin\varphi; \\ Z_{D} &= X_{ID}\sin\Theta\sin\varphi + Y_{ID}\sin\Theta\cos\varphi + Z_{ID}\cos\Theta. \end{split}$$

For  $\delta = 0$  tool coordinates will take the form:

$$X_{ID}=0, Y_{ID}=-R_u, Z_{ID}=0.$$
 (23)

In this case the equations of tool motion depending on the angle of rotation  $\psi$  of the main shaft will be:

$$X_{D} = -R_{u}(1 - \cos\Theta)\cos\varphi\sin\varphi,$$

$$Y_{D} = -R_{u}(\sin^{2}\varphi + \cos\Theta\cos\varphi),$$

$$Z_{D} = -R_{u}\sin\Theta\cos\varphi.$$
(24)

In the case of toothed wheels with angle  $\delta > 0$  the tool should be located under the same angle. Then point D will have the following coordinates:

$$X_{ID}=0, Y_{ID}=-R\cos\delta,$$

$$Z_{ID}=-R\sin\delta,$$
(25)

And the equations of the path of motion of tool in the fixed system of coordinates OXYZ have the form:

$$\begin{split} X_{D} &= -R_{u}\cos\delta(1-\cos\Theta)\cos\varphi\sin\varphi - R_{u}\sin\delta\sin\Theta\sin\varphi;\\ Y_{D} &= -R_{u}\cos\delta(\sin^{2}\varphi + \cos\Theta\cos\varphi) + R_{u}\sin\delta\sin\Theta\cos\varphi;\\ Z_{D} &= -R_{u}\cos\delta\sin\Theta\cos\varphi - R_{u}\sin\delta\cos\Theta. \end{split}$$

(26)

Exact performance of the tool path of motion was taken into account in the process of elaboration of the tool-carrier device, shown in fig. 1.

## 2.2.3. Technological equipment for generating teeth with sfero-space motion of truncated cone shaped tool

The profile of central wheel tooth of precessional gear is variable depending on the values of conical axoid angle  $\delta$ , taper angle of the rollers  $\beta$ , the nutation angle  $\theta$ , the number of teeth of gears  $Z_1,Z_2$  and the correlation between them. Fabrication of these profiles using traditional methods is practically impossible, because for each correlation value of all parameters  $\delta$ ,  $\beta$ ,  $\theta$  and Z tooth profile changes shape, which requires the design and manufacture of the tool with the respective profile.

Therefore a new generating technology was proposed, which carries out a set of profiles of the teeth, using a tool with the same geometrical parameters. The method consists of the following: a series of motions coordinated between them against the rotating blank is communicated to the tool (milling cutter or grinding wheel with truncated cone-shaped geometry). The kinematic link of the blank with the tool provides rotation of one-toothed blank in a closed cycle of the motion communicated to the tool. The tool is given such a shape and motion that allows the processing of any possible profile of the set, including longitudinal and profile modification. The described surface on the peripheral side of the tool against the rotating blank reproduces a certain conceivable body, called the imaginary wheel (generators).

Using the kinematic chain of gear cutting machine-tool running, gear blank and the tool are brought in a coordinated motion – running motion, which reproduces the imaginary wheel gearing with

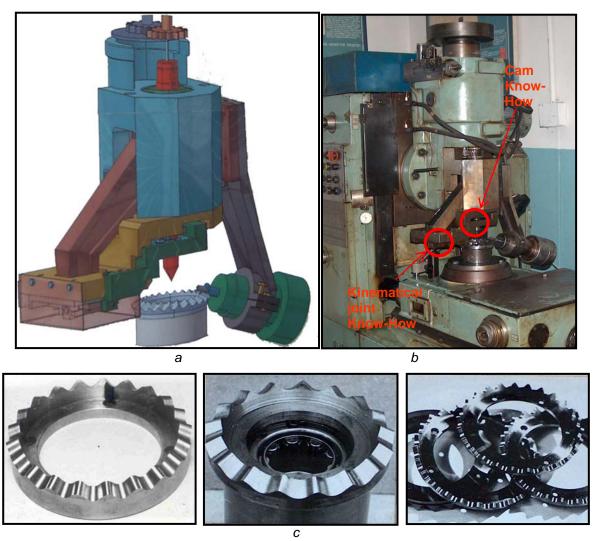
the blank. Part of metal is removed at each elementary change of tool position in space in relation to the blank. Therefore the working surface of the wheel teeth processed is obtained as envelope of a consecutive series of positions of rotating tool profile generator contour against the blank.

A tool holder device was developed to realize the demanded motions of the tool (Fig. 4, a), which can be adjusted to gear cutting machines models 5K32P53, 5330P, 53A50, 5A60, 5342, with accuracy class GOST 6-77.

To compensate error diagram of the satellite at its sphere-spatial rotation, a kinematical joint connecting the cross-rail with the body is introduced into the teeth grinder, ensuring continuity of the transformation function of rotational motion  $\omega_I/\omega_3 = const.$  in the kinematic chain "main shaft - tool - blank". In other words, at teeth processing by proposed method, their profile is corrected by an amount equal to the kinematical diagram error introduced by the sphere-spatial motion of tool with regard to the casing (bed).

It was defined that in real precessional transmissions 2K-H the link of precessional satellite with the body introduces an error in the driven shaft position. This fact provokes non-uniformity of its rotation at uniform turning of the drive shaft. Drawback is eliminated by transposition of driven shaft position error on the processed tooth profile. Diagram error elimination is achieved through the construction of cross-rail connection joint to the body, which through a cam installed on the crank shaft communicate auxiliary motion to the tool. The joint ensures continuity to the transformation function of rotational motion along the linkage shaft-crank-tool-blank. At tooth processing by proposed method their profile is correlated to value of the shift angle of driven shaft introduced by precessional satellite link in the real transmission. In the developed tool-carrier device the point of intersection of the fixed axis OZ with the movable axis  $OZ_I$  of the crank (centre of precession) is on the axis of rotation of the gear cutting machine table. To research the features of interaction between the tool and the wheel processed tooth ( $\delta$ > 0), which axis coincides with axis OZ of the device crank-shaft:

Fig. 4, a shows the 3D computer model of the processing device for gear wheels with non-standard profile, designed in *AutoDeskInventor* and simulated in *MotionInventor*. Fig. 4, b shows the picture of gear cutting machine-tool endowed with the device for profile generation by precessional tool. Fig. 4, c presents samples of gear wheels with non/standard profile, worked out on this machine-tool.



**Figure 4.** Generation device for gears with non-standard profile (a), machine-tool with fabricated device (b) and samples of fabricated gears (c)

#### 4. CONCLUSIONS

Among the characteristics of the estimated results of research in the field of new and efficient drive development we can enumerate the following:

- the elaborated precessional gears ensure: high bearing capacity; high kinematical efficiency; high kinematical accuracy; low noise level and vibrations;
- generation procedure for variable convexconcave teeth profiles provide high efficiency and processing accuracy.

Structural optimization of the precessional transmissions will allow synthesis of new diagrams of precessional transmissions with constant and variable transmission ratio and elaboration of new diagrams of precessional transmissions for specific running conditions.

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