

Ferromagnetic Josephson junctions with steplike interface transparencyN. G. Pugach,^{1,*} M. Yu. Kupriyanov,² A. V. Vedyayev,¹ C. Lacroix,³ E. Goldobin,⁴ D. Koelle,⁴ R. Kleiner,⁴ and A. S. Sidorenko^{5,6}¹*Faculty of Physics, M.V. Lomonosov Moscow State University, 119992 Leninskie Gory, Moscow, Russia*²*Nuclear Physics Institute, M.V. Lomonosov Moscow State University, 119992 Leninskie Gory, Moscow, Russia*³*Institut Néel, CNRS-UJF, BP 166, 38042 Grenoble Cedex 9, France*⁴*Physikalisches Institut-Experimentalphysik II and Center for Collective Quantum Phenomena, Universität Tübingen, Auf der Morgenstelle 14, D-72076 Tübingen, Germany*⁵*Institute of Electronic Engineering and Industrial Technologies, ASM, MD2028 Kishinev, Moldova*⁶*Institute of Nanotechnology, Karlsruhe Institute of Technology (KIT), D-76021 Karlsruhe, Germany*

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Within the framework of the quasiclassical Usadel equations we study the Josephson effect in superconductor-insulator-ferromagnet-superconductor (SIFS) and SIFNS (N is a normal metal) structures with a steplike transparency of the FS or NS interface. At certain parameters the steplike transparency leads to the formation of a region, where the critical current-density distribution $J_C(y)$ along the junction exhibits a damped oscillation with a sign change. This results in the formation of a $0-\pi$ nanojunction with the characteristic length of 0 and π regions of the order of the coherence length ξ_F for SIFS and ξ_N for SIFNS junctions, respectively. Using several transparency steps one can create an array of nanojunctions. Such structures exhibit an unusual behavior in an external magnetic field H . The total critical current grows with increasing H up to a certain value, which depends on the size of a single nanojunction, and has multiperiodic oscillations in the case of an array.

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I. INTRODUCTION

Recently, unconventional properties of Josephson junctions (JJs) have attracted a lot of attention.¹⁻³ Contrary to the already well-known 0 JJs with a Josephson phase $\varphi=0$ in the ground state, junctions with ferromagnetic barriers may have a ground state with $\varphi=\pi$ (π -JJs). These junctions may be used in electronic circuits, e.g., in JJ flux qubits with low decoherence,⁴ self-biased rapid single flux quantum digital circuits,⁵ or complementary logic.⁶ If the current-phase relation of a JJ has the usual form $J(\varphi)=J_C \sin(\varphi)$ the ground state $\varphi=0$ is realized for $J_C>0$ and the ground state $\varphi=\pi$ for $J_C<0$. The last condition may be satisfied in the case of a ferromagnetic barrier. Such a junction consists of two superconducting electrodes (S) separated by the ferromagnetic layer (F). It could include also a thin insulating tunnel barrier (I), i.e., SFS or SIFS multilayers may be considered.

Modern technology allows to manufacture not only 0 or π -JJs but also the so-called $0-\pi$ Josephson junctions, i.e., junctions some parts of which behave as 0 junctions and other parts behave as π junctions.⁷ In these structures, intensively studied experimentally, the different sign of J_C can be achieved by introducing a steplike change in the thickness of the F layer.⁸⁻¹²

The interest in these structures has been stimulated by the existence of unusual topological vortex solutions in these $0-\pi$ junctions. A spontaneous Josephson vortex carrying a fraction of the magnetic-flux quantum $\Phi_0 \approx 2.07 \times 10^{-15}$ Wb may appear at a $0-\pi$ boundary.^{7,13,14} In the region, where the phase φ changes from 0 to π , there is a nonzero gradient $\partial\varphi/\partial y$ of the Josephson phase along the junction that is proportional to the local magnetic field. In essence this field is created by supercurrents $\sim \sin(\varphi)$ circu-

lating in this region. These currents are localized in a λ_J vicinity of the $0-\pi$ boundary (λ_J is the Josephson penetration depth) and create a vortex of supercurrent with total magnetic flux equal to $\pm\Phi_0/2$, whereas a usual Josephson vortex carries $\pm\Phi_0$, provided that the junction length $L \gg \lambda_J$. In the case of $L \lesssim \lambda_J$ the spontaneous flux^{7,13,15-17} $|\Phi| < \Phi_0/2$. It was shown theoretically^{17,18} and indicated in experiments⁹⁻¹¹ that for certain conditions the existence of a fractional Josephson vortex at the $0-\pi$ boundary is energetically favorable in the ground state. The fractional vortex is pinned at the $0-\pi$ boundary and has two polarities that may be used for information storage and processing in the classical and quantum domains, e.g., to build JJ-based qubits.¹⁹ We note that the fractional vortex described above is always pinned and is different from fractional Josephson vortices that are the solutions of a double sine-Gordon equation.²⁰⁻²²

Not only single Josephson junctions but also superconducting loops intersected by two JJs [dc superconducting quantum interference devices (SQUIDs)] and their arrays may be used in applications. Such arrays consist of N Josephson junctions connected as a one-dimensional parallel chain in such a way that $N-1$ individual superconducting loops are formed. Such an array exhibits an unusual dependence of its mean voltage on the magnetic field H for overcritical applied bias current. If the loops are identical the voltage response $V(H)$ is Φ_0 periodic. For JJ arrays with incommensurate loop areas the voltage response $V(H)$ is nonperiodic, and can have a rather sharp dip at $H=0$. This property may be used to create a sensitive absolute field magnetometer that is called superconducting quantum interference filter (SQIF).²³⁻²⁷ So far, these SQIFs are based on usual JJs. However, recently it was also suggested to realize $0-\pi$ SQIFs, using constriction junctions in d -wave superconductors.²⁸ In the present paper we suggest SQIF-like